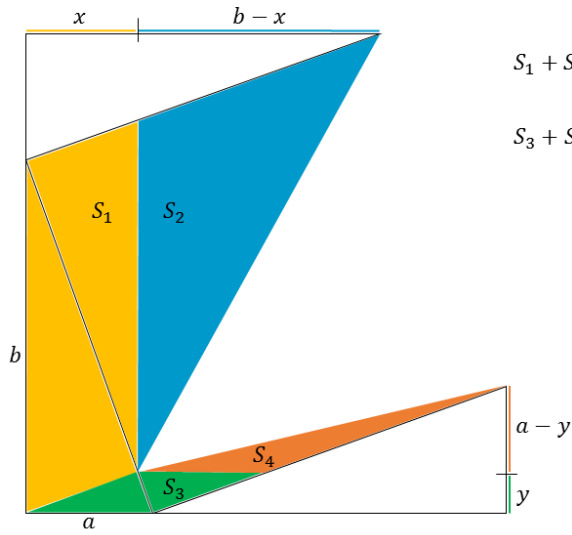
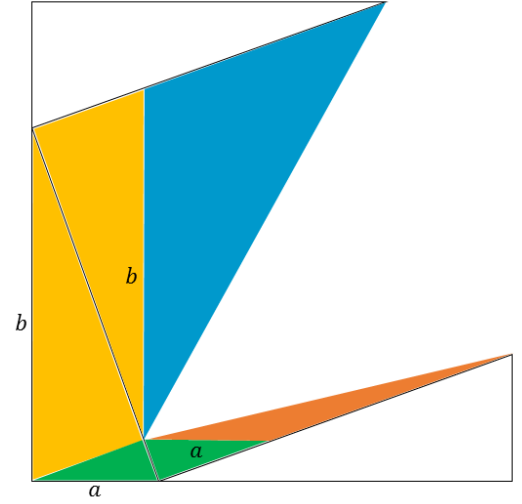
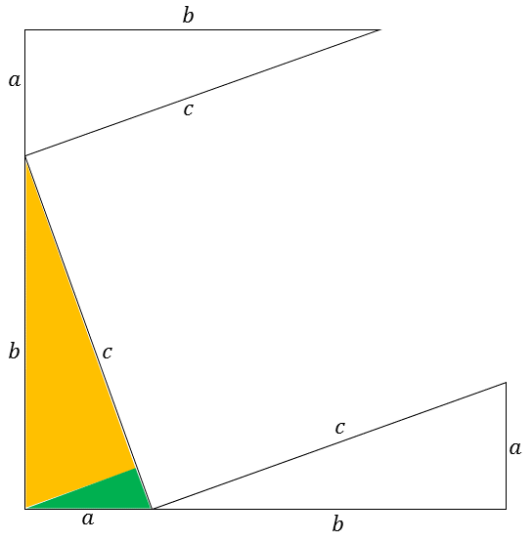
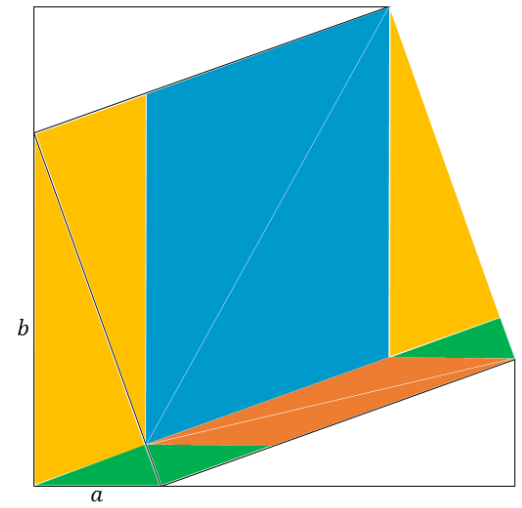


Pythagorean Theorem Proof #1 | Gil Brand, 2015

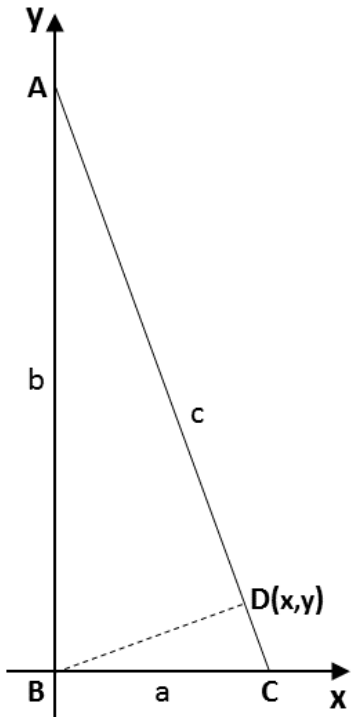


$$S_1 + S_2 = \frac{bx}{2} + \frac{b(b-x)}{2} = \frac{b^2}{2}$$

$$S_3 + S_4 = \frac{ay}{2} + \frac{a(a-y)}{2} = \frac{a^2}{2}$$



Pythagorean Theorem Proof #2 | Gil Brand, 2015



$$AC \perp BD$$

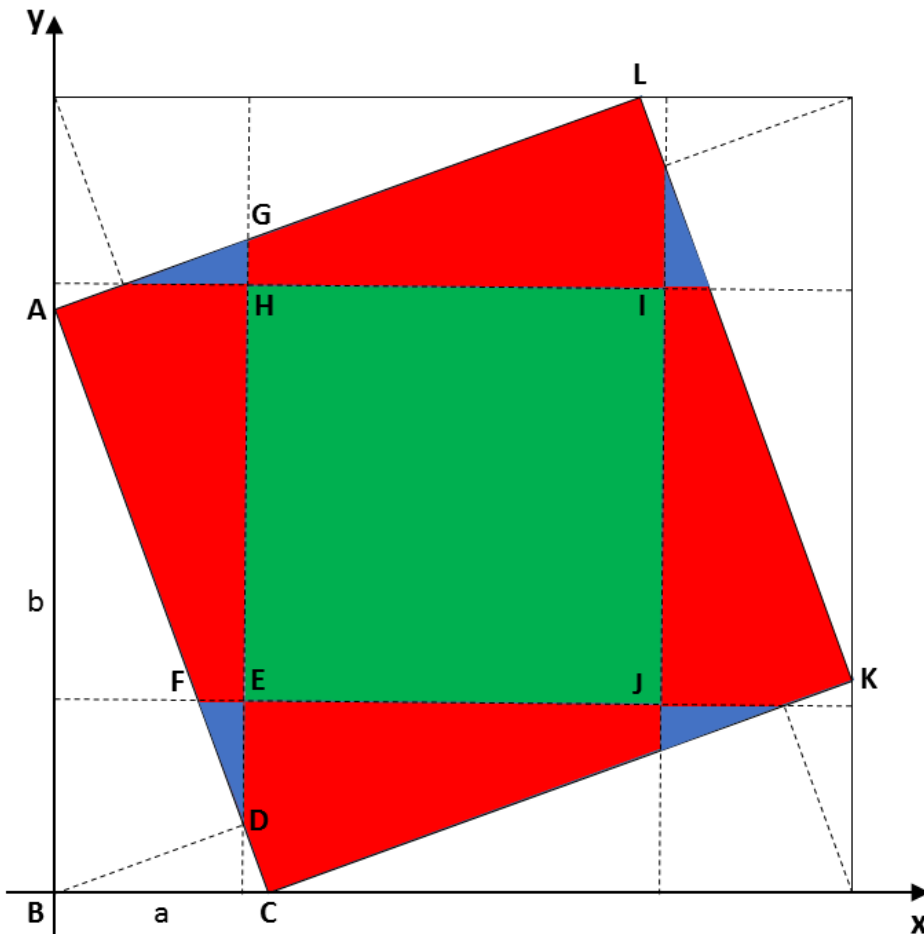
$$AC: y = -\frac{b}{a}x + b$$

$$BD: y = \frac{a}{b}x$$

Intersection Point D:

$$-\frac{b}{a}x + b = \frac{a}{b}x$$

$$x = \frac{ab^2}{a^2 + b^2} ; y = \frac{a^2b}{a^2 + b^2}$$



ΔDAG

Parallelogram ABDG: $DG = b$

$$S_{DAG} = \frac{DG \cdot x}{2} = \frac{bx}{2} = \frac{ab^3}{2(a^2 + b^2)}$$

$\Delta ABC \sim \Delta DEF$

$$\frac{S_{ABC}}{S_{DEF}} = \left(\frac{b}{DE}\right)^2 \rightarrow \frac{\frac{ab}{2}}{S_{DEF}} = \left(\frac{b}{x-y}\right)^2$$

$$S_{DEF} = \frac{a(ab^2 - a^2b)^2}{2b(a^2 + b^2)^2}$$

Square EJIH:

$$EJ = a + b - 2x = a + b - \frac{2ab^2}{a^2 + b^2}$$

$$S_{EJIH} = EJ^2 = \left(a + b - \frac{2ab^2}{a^2 + b^2}\right)^2$$

Square ACKL:

$$S_{ACKL} = c^2 = 4(S_{DAG} - S_{DEF}) + S_{EJIH}$$

$$c^2 = 4\left(\frac{ab^3}{2(a^2 + b^2)} - \frac{a(ab^2 - a^2b)^2}{2b(a^2 + b^2)^2}\right) + \left(a + b - \frac{2ab^2}{a^2 + b^2}\right)^2$$

$$c^2 = \frac{(a^2 + b^2)^3}{(a^2 + b^2)^2} = a^2 + b^2$$